

# Mitigation of Signal Diffraction Effects on Precise GPS-Positioning

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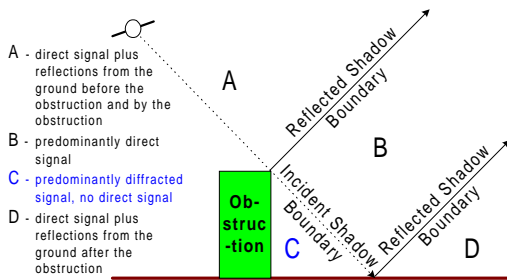
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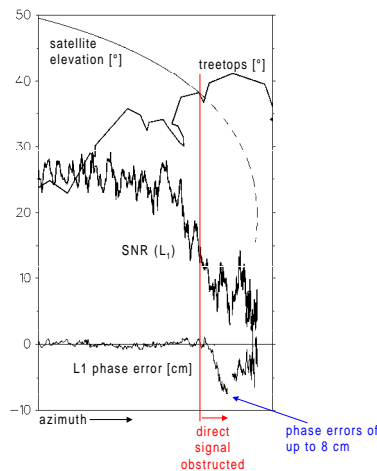
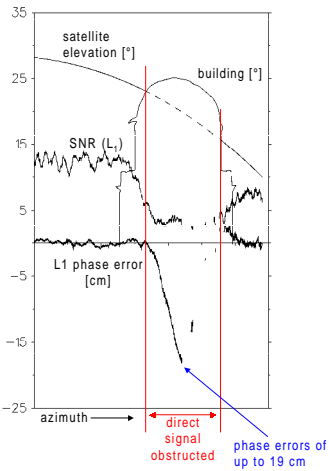
Signal diffraction is a common error source in precise GPS positioning if obstructions exist above the antenna horizon. It occurs whenever the direct signal is obstructed but nevertheless a diffracted signal is received and processed. The longer propagation time of a diffracted signal causes carrier phase errors of up to several cm. A common characteristic of all diffracted signals is their weak signal power as compared to a direct signal received under the same elevation angle.

In the case of Trimble GPS-receivers, the signal strength is given as SNR (signal-to-noise values of the  $L_1$  and  $L_2$  phase observations) in arbitrary, i.e. Trimble-specific, units. In order to be able to process these secondary observables, we extended our post-processing software Wa-Soft:

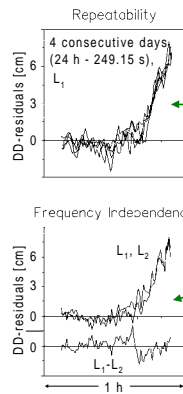
- ... to include Trimble-SNR values in the RINEX observation files according to RINEX version 2.1,
- ... to include weighting functions which are based on SNR values.



**Examples of diffraction effects on phase observations and signal strength**

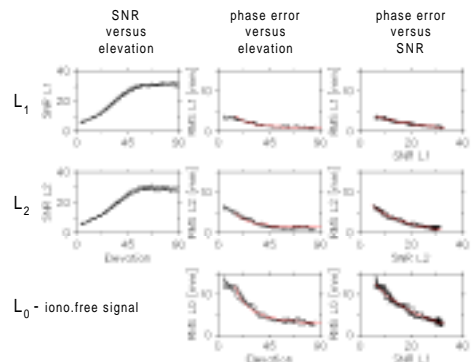


## Comparison: Diffraction Effects, Multipath Effects



	Diffraction Effects	Multipath Effects
<b>Common Features</b>	<ul style="list-style-type: none"> <li>depends on local environment of receiving antenna,</li> <li>repeats with identical satellite constellation and unchanged environment,</li> <li>no mitigation by relative positioning,</li> <li>the effect on coordinate estimation is reduced with increase of observation time (static observations),</li> <li>in kinematic mode rapid changes of the local environment and thus rapid changes of diffraction effects: mitigation by filtering.</li> </ul>	
<b>Differences</b>	<ul style="list-style-type: none"> <li>no line-of-sight signal, only diffracted signal received,</li> <li>independent of signal frequency: geometry-free linear combination not affected,</li> <li>maximum errors: in the order of decimeters,</li> <li>signal strength reduced.</li> </ul>	<ul style="list-style-type: none"> <li>superposition of direct and reflected (indirect) signals,</li> <li>frequency-dependent: detection in geometry-free linear combination,</li> <li>maximum errors: 4.8 cm L1, 6.1 cm L2, 21.4 cm ionospheric-free combination,</li> <li>fluctuating signal strength</li> </ul>

## Analysis of Trimble phase data / Weighting functions



**weighting functions**  
(best fitting functions shown in red):

elevation-dependent weighting:  
 $w(e) = \sin^2(e)$   
 for  $e > 10$  deg

SNR-dependent weighting:  
 $w(SNR) = e^{SNR/A}$   
 with  $A(L_1) = 10$ ,  
 $A(L_2) = 6$ ,  
 $A(L_0) = 9$

## Elevation-dependence of Trimble-SNR-values:

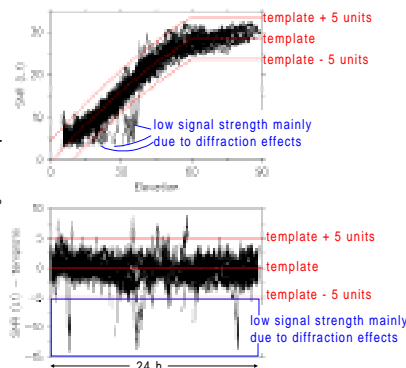
Trimble 4000 SSE / 4000 SSI / 4700 / 4800 - receivers: SNR given in arbitrary units (receiver-dependent)

$$\text{template}(e) = a_0 + a_1 \cdot e + a_2 \cdot e^2 \quad \text{for } 0^\circ < e < 60^\circ$$

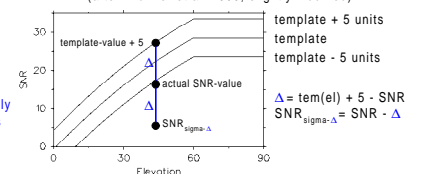
$$a_0 + a_1 \cdot 60 + a_2 \cdot 60^2 \quad \text{for } e > 60^\circ$$

iterative calculation with elimination of SNR-values < template - 5 units,

individual templates for each receiver-antenna pair: differences up to 10 units

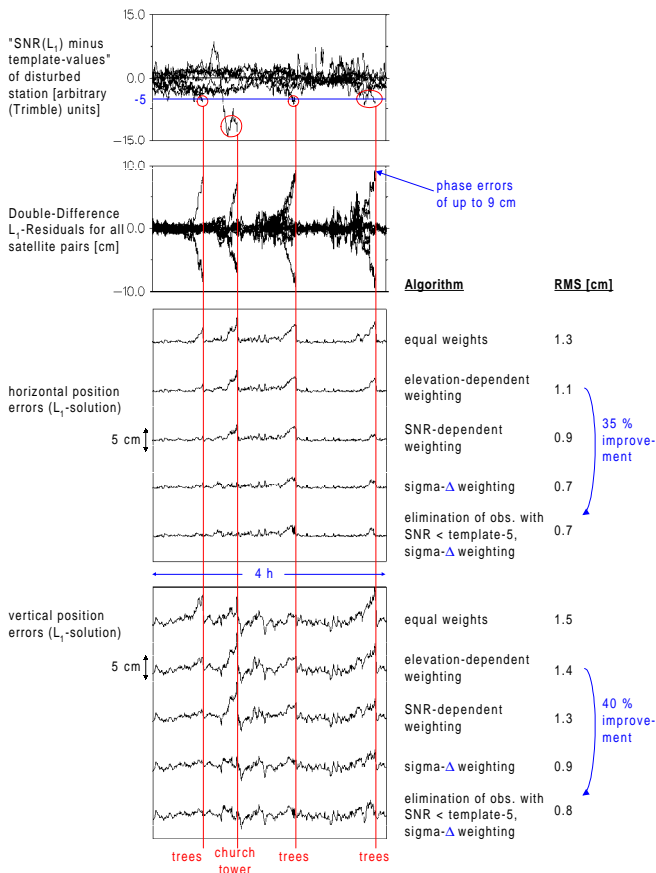


**sigma- $\Delta$  weighting: SNR-dependent weighting using SNR**  
(after Brunner et al. 1999, slightly modified)



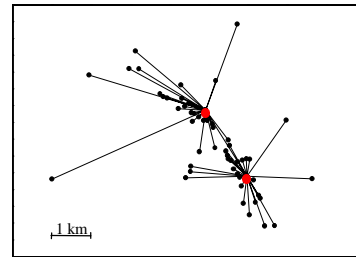
## Kinematic Processing of a Static Baseline

baseline length 3 km, one station affected by signal diffraction



## Rapid Static Positioning

network of 55 stations, 5 km x 6 km, two independent determinations, session lengths 10 minutes with minimum of 5 SVs, two permanent stations, rural area: signal obstructions by trees, buildings etc.



Algorithm	all 55 stations		11 stations with diffraction effects	
	horizontal	vertical	horizontal	vertical
equal weights	1.6	2.2	2.4	1.9
elevation-dependent weighting	1.3	1.9	2.1	2.1
SNR-dependent weighting	1.2	1.8	1.9	2.0
sigma- $\Delta$ weighting	1.0	1.6	1.4	1.7
sigma- $\Delta$ weighting + cleaning	0.9	1.5	1.3	1.6

RMS of coordinate differences [cm] between two independent network determinations.

20 ... 40 % improvement  
cleaning - elimination of those 5 % of observations which cause the largest double-difference residuals (applicable to static observations only).

## Results and Conclusions:

Phase errors due to signal diffraction can reach several cm. Most diffraction events are detectable in the signal-to-noise (SNR) values, if the elevation-dependence of SNR values are taken into account.

A slightly modified sigma- $\Delta$  weighting algorithm (after Brunner et. al 1999) improves kinematic and rapid static positioning results by 20 to 40 %.

Kinematic positioning can be further improved by elimination of those observations whose SNR values indicate large diffraction effects. Rapid static results gain by elimination of those 5 % of observations which cause the largest double-difference residuals.