



**TECHNISCHE
UNIVERSITÄT
DRESDEN**



Fakultät Verkehrswissenschaften „Friedrich List“

Professur für Bahnverkehr, öffentlicher Stadt- und Regionalverkehr



Public Transport Operations and Supply

Development of rotating duty rosters

Dipl.-Ing. Steffen Dutsch



Technische Universität Dresden



18 faculties in five schools:



Mathematics und Natural Sciences



Humanities and Social Sciences



Medicine



Engineering Sciences



Civil and Environmental Engineering

**Faculty of Transport and Traffic Sciences
„Friedrich List“**

7 institutes, 22 chairs

36.000 students and 6000 employees

Structure of the faculty

Institute of Transport Planning and Road Traffic

Institute of Traffic Telematics

Institute of Logistics and Aviation

Institute of Railway Vehicles and Railway Technology

Institute of Transport & Economics

Dresden Institute of Automobile Engineering

Institute of Railway Systems and Public Transport

Founded in: 1992
Professors: 22
Students: ≈1500

Structure of the institute

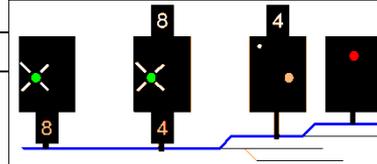
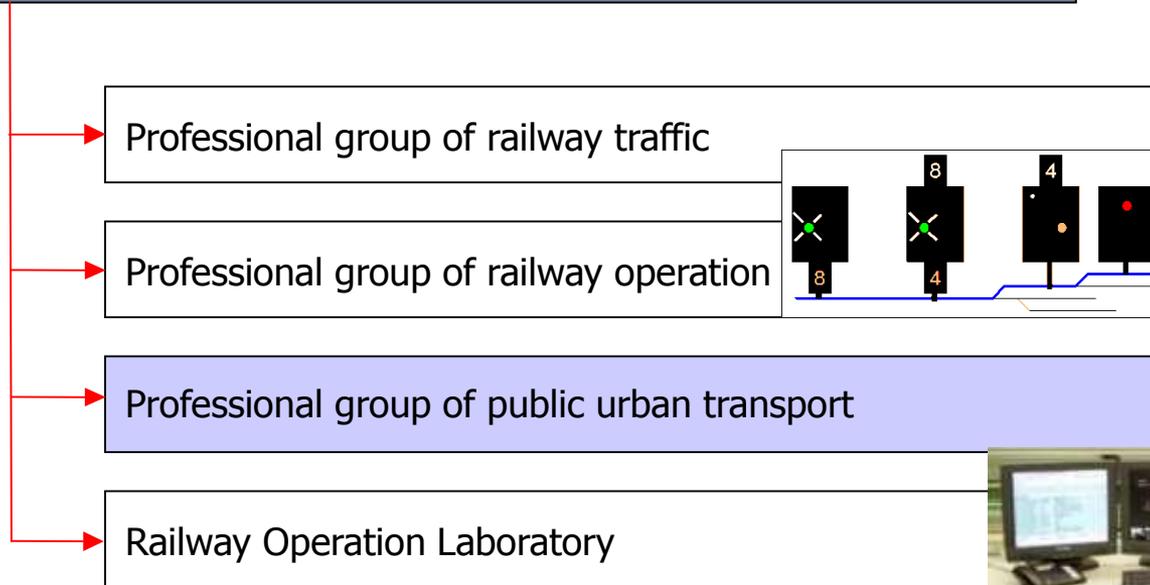
Chair of Transportation Systems Engineering

Chair of Planning and Design of Railway Infrastructure

Chair of Rail and Public Urban Transport

Chair of Railway Signalling and Transport Safety Technology

Structure of the chair



Public Transport Operations and Supply

Development of rotating duty rosters

1. Introduction

- 1.1. Task and steps of duty-scheduling
- 1.2. Tasks and problems of duty-rostering
- 1.3. Types of duty rosters

2. Development of rotating duty rosters

- 2.1. Duty rosters with fixed cycle
- 2.2. Duty rosters with weekly cycle

3. General examples

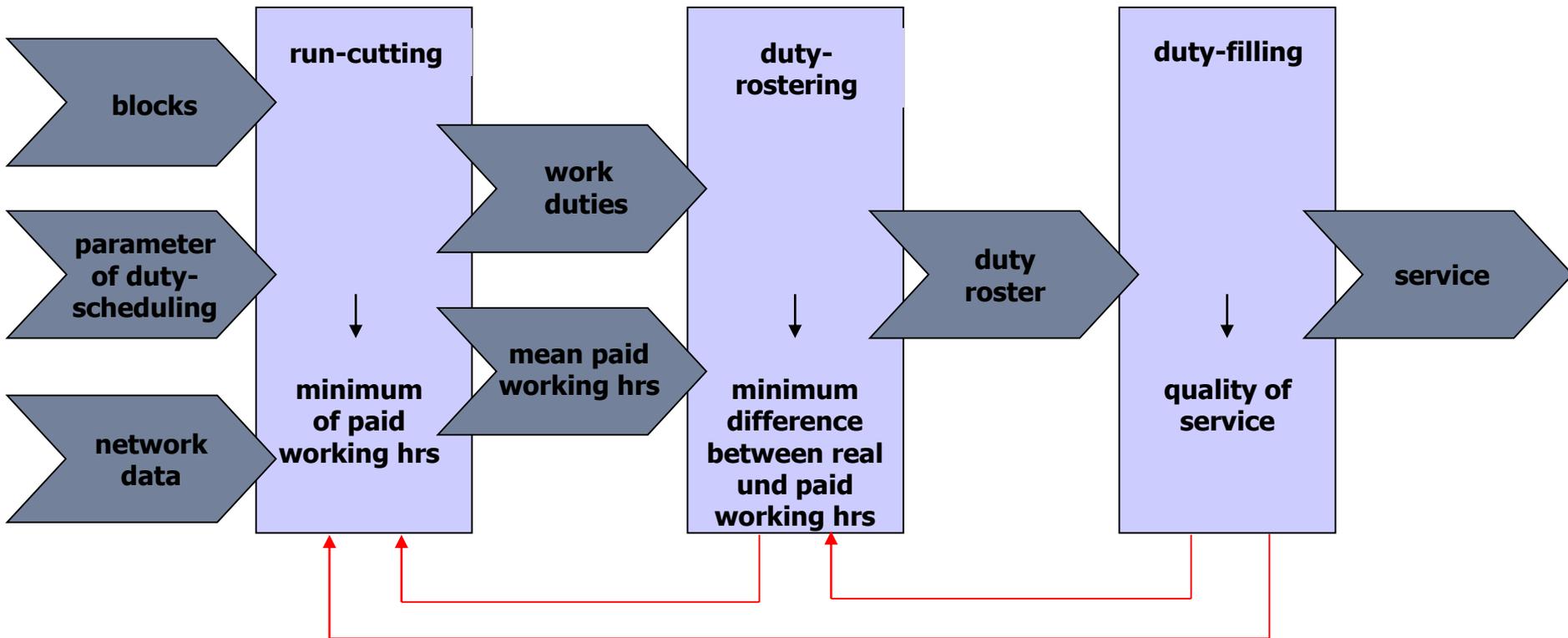
- 3.1. Shift similarly duty roster
- 3.2. Duty roster with fast rotation

4. Exercise

Public Transport Operations and Supply

Development of rotating duty rosters

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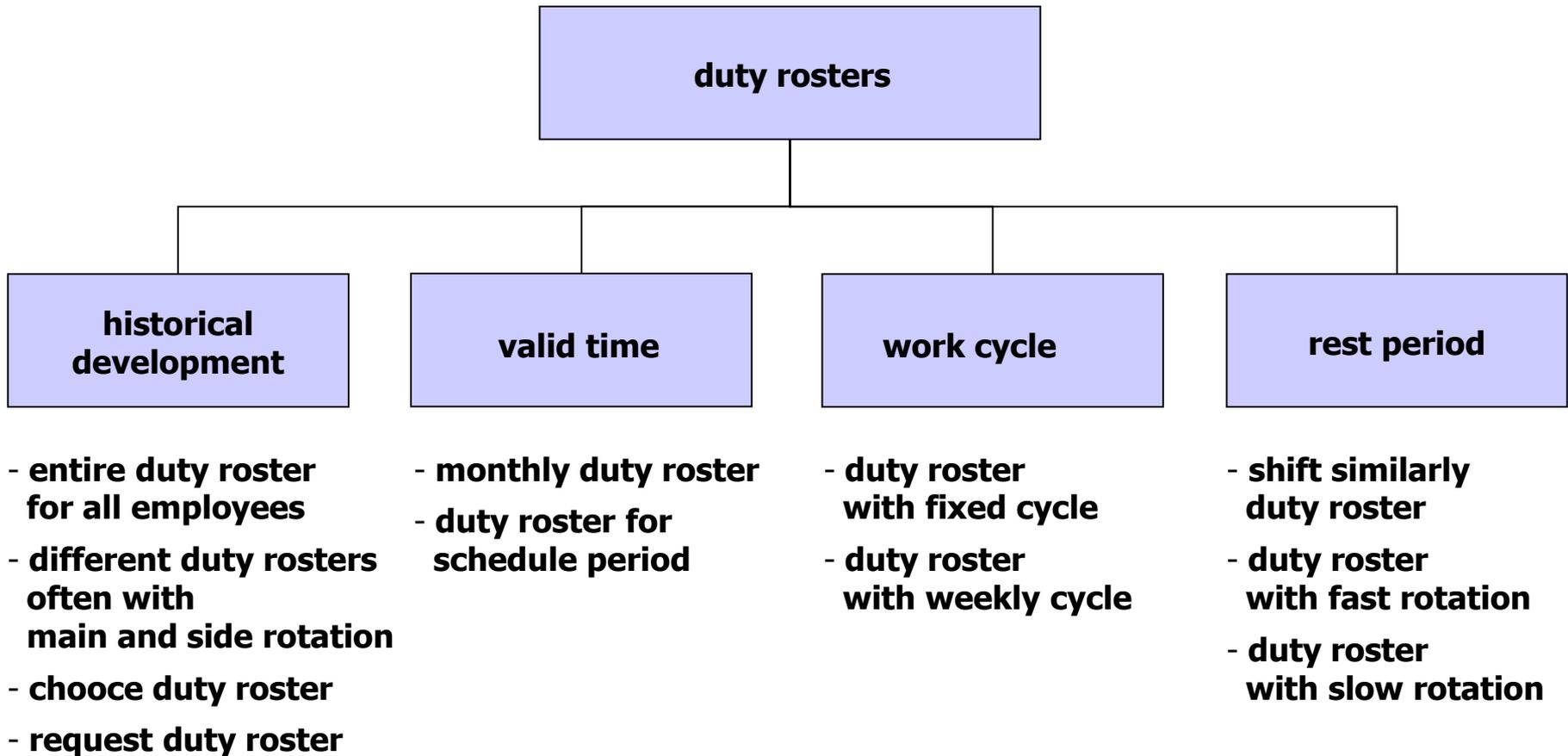
Task:

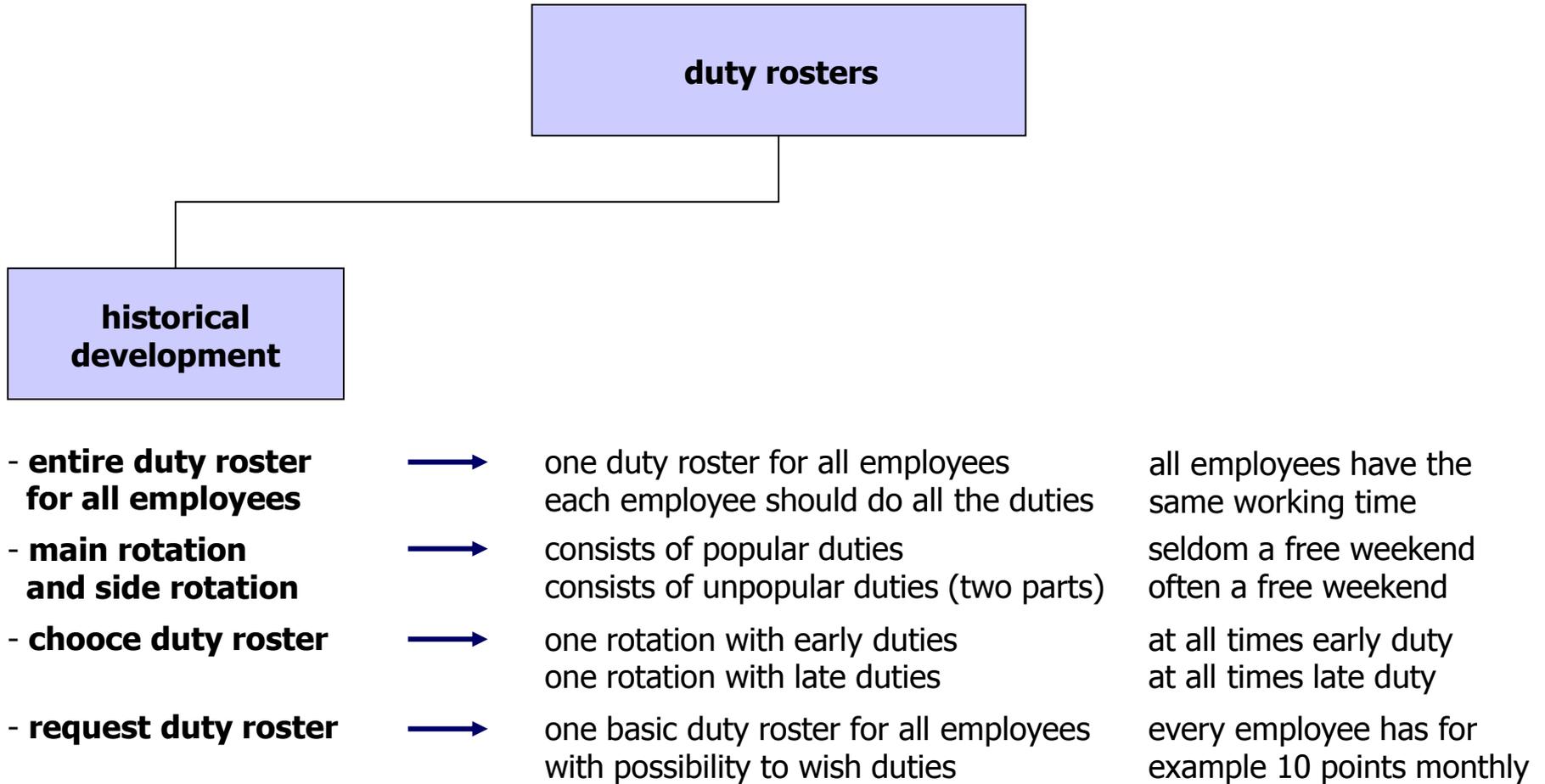
group all duties and days-off into a roster, that is

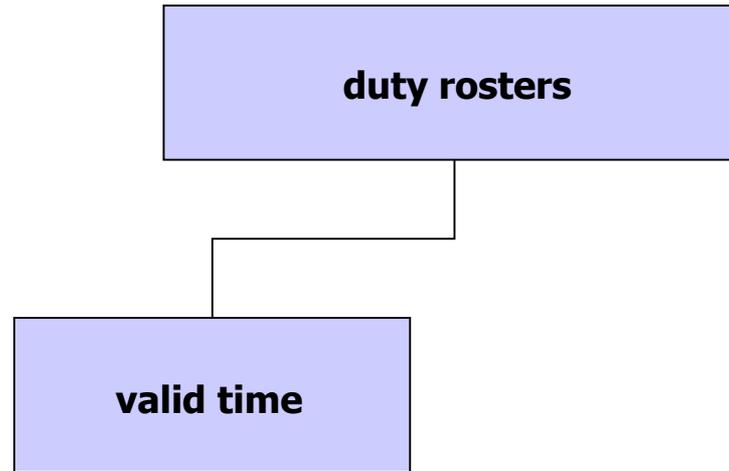
- with exactly one employee per duty each day
- in compliance with the law
- as social as possible

Problems:

- Different number of duties at different days (monday to friday, saturday and sunday)
- minimal rest period: 10 hours
maximal number of duties without days-off: 6 duties
minimal number of free sundays per year: 15 sundays
- Number of cycledays, sum of duties and days-off should be between 4 and 8 days but never 7 days







- **monthly
duty
roster**



regional transport, public urban transport in small networks

without any cycle

possibility to take bank holidays, special features or wishes into account

- **duty roster
for schedule
period**

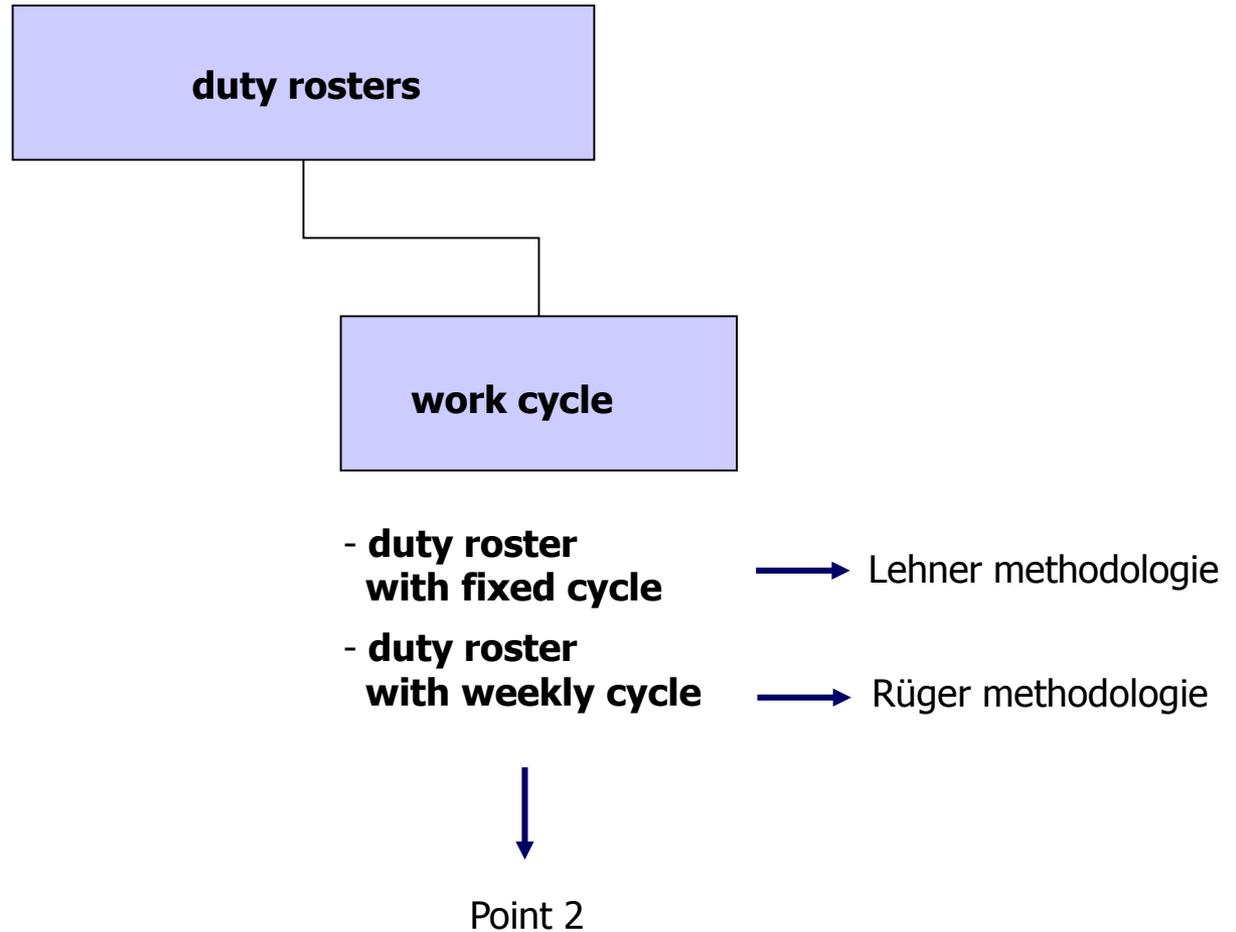


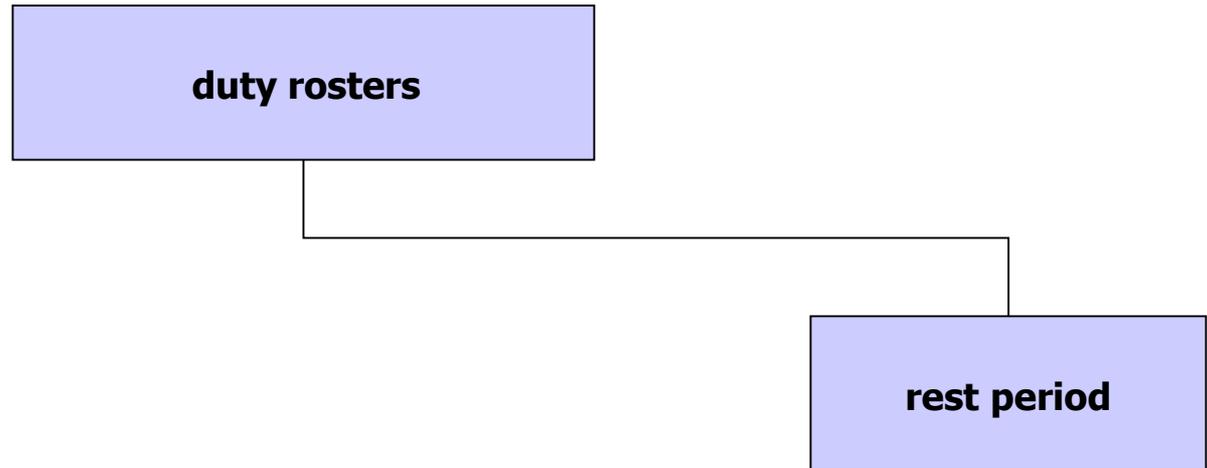
rail transport, public urban transport in large networks

with fixed or weekly cycle

no possibility to take bank holidays, special features or wishes into account;

this possibility exists only in the step duty-filling





second duty begins and ends about 24 hours after the first
best possibility for families with children

second duty begins and ends less than 24 hours after the first
popular with young people

second duty begins and ends more than 24 hours after the first
best possibility for elderly employees ¹⁾

- ← - **shift similarly
duty roster**
- ← - **duty roster
with fast rotation**
- ← - **duty roster
with slow rotation**

¹⁾ reference:
 Tarifvertrag zur Bewältigung des
 demografischen Wandels im Nahverkehr.-
 Vereinigung der kommunalen
 Arbeitgeberverbände (VKA), 2013

¹⁾ reference:
 collective agreement to overcome
 demographic change in public transport.-
 Union of Employers' Associations, 2013
 enacts January, 1 2014

Transportation systems (M. Sc.)

Development of rotating duty rosters

- 1. Introduction**
 - 1.1. Task and steps of duty-scheduling
 - 1.2. Tasks and problems of duty-rostering
 - 1.3. Types of duty rosters
- 2. Development of rotating duty rosters**
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 - 3.2. Duty roster with fast rotation
- 4. Exercise**

4 working days and 2 days-off

weekday	1	2	3	4	5	6	7	1	2	3	4	5	6	7	1	2	3	4	5	6	7	1	2	3	4	5	6	7	1	2	3	4	5	6	7		
cycleday	1	2	3	4	5	6	1	2	3	4	5	6	1	2	3	4	5	6	1	2	3	4	5	6	1	2	3	4	5	6	1	2	3	4	5	6	7
staff no. 1	■	■					■	■	■				■	■					■	■							■	■			■	■					
staff no. 2		■	■	■					■	■	■								■	■							■	■			■	■					
staff no. 3			■	■	■					■	■	■							■	■							■	■			■	■					
staff no. 4				■	■	■					■	■	■						■	■							■	■			■	■					
staff no. 5					■	■	■					■	■	■					■	■							■	■			■	■					
staff no. 6	■					■	■					■	■	■					■	■							■	■			■	■					

4 working days and 1 day-off

weekday	Mo	Tu	We	Th	Fr	Sa	Su	Mo	Tu	We	Th	Fr	Sa	Su	Mo	Tu	We	Th	Fr	Sa	Su	Mo	Tu	We	Th	Fr	Sa	Su							
cycleday	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5					
staff no. 1	■					■						■				■				■							■			■					
staff no. 2		■					■					■					■			■							■			■					
staff no. 3			■						■				■					■			■							■			■				
staff no. 4				■						■				■						■								■			■				
staff no. 5					■						■					■				■							■			■					

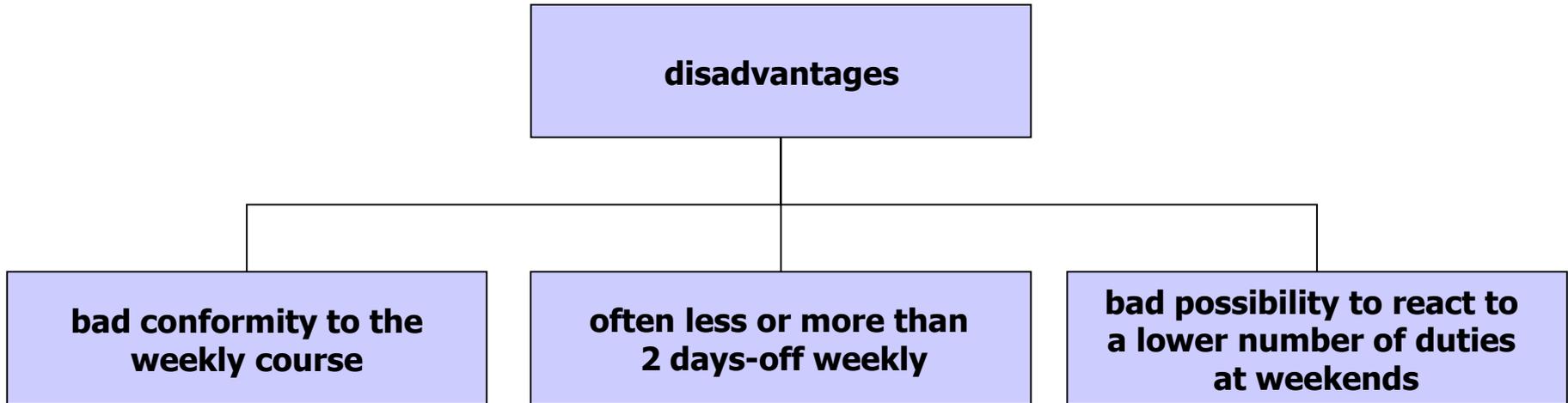
weekday	Mo	Tu	We	Th	Fr	Sa	Su	Mo	Tu	We	Th	Fr	Sa	Su	Mo	Tu	We	Th	Fr	Sa	Su	Mo	Tu	We	Th	Fr	Sa	Su							
cycleday	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5					
staff no. 1	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■	■					
staff no. 2	■					■						■				■				■							■			■					
staff no. 3		■					■					■					■			■							■			■					
staff no. 4			■						■				■					■			■							■			■				
staff no. 5				■							■					■				■							■			■					

■ day-off

□ duty

■ ■ □ □ □ □ cycle basis group of 6 days

Mo	Tu	We	Th	Fr	Sa	Su
				■		
■		■			■	
			■			
■	■					■



- wife, husband
- children
- leisure time activities
- opening times ...

- extra short duties
- extra long duties

- to much employees on Saturday and Sunday
- not enough employees from Monday to Friday

—————> **duty roster with weekly cycle**

—————> **consists of frame basic groups with two days-off weekly**

Number of week	su	mo	tu	we	th	fr	sa
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B 1 (1 week, 1 cycle basis group, 2 days-off)

1.	day-off						day-off
----	---------	--	--	--	--	--	---------

B 3 (3 weeks, 4 cycle basic groups, 6 days off)

1.	(day-off)				day-off	day-off	
2.				day-off	↓		
3.		day-off	day-off				(day-off)

(day-off)

extra day-off, either Saturday or Sunday day-off, with the possibility to move it in the next week

day-off



B 4 (4 weeks, 5 cycle basic groups, 8 days-off)

1.	day-off					day-off	(day-off)
2.				day-off	day-off		
3.			day-off	↓			
4.	(day-off)	day-off					day-off

B 6 (5) (6 weeks, 5 cycle basic groups, 12 days-off)

1.	day-off	day-off					
2.		day-off	day-off				
3.			day-off	day-off			
4.				day-off	day-off		
5.					day-off	day-off	
6.						day-off	day-off

B 6 (7) (6 weeks, 7 cycle basic groups, 12 days off)

1.	<day-off>				<day-off>	day-off	<day-off>
2.				<day-off>	day-off	<day-off>	
3.			<day-off>	day-off	<day-off>		
4.		<day-off>	day-off	<day-off>			
5.	<day-off>	day-off	<day-off>				<day-off>
6.	day-off	<day-off>				<day-off>	day-off

<day-off>

extra day-off, take only 5 from there

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number of week	shift	su	mo	tu	we	th	fr	sa
B_e								
1.	e	day-off	e	e	e	e	e	day-off
B_l								
1.	l	day-off	l	l	l	l	l	day-off
$B_{e/l}$								
1.	e	day-off	e	e	e	e	day-off	l
2.	l/e	l	l	l	day-off	day-off	e	e
3.	l	e	day-off	day-off	l	l	l	l
$B_{l/e}$								
1.	l	l	l	l	l	day-off	day-off	e
2.	e/l	e	e	e	day-off	l	l	l
3.	e	l	day-off	day-off	e	e	e	day-off

e early shift
l late shift

it goes:

$$\begin{aligned}
 n_{B_e} &= n_{emf} - k \\
 n_{B_l} &= n_{lmf} - k \\
 n_{B_{e/l}} &= n_{lsa} - k \\
 n_{B_{l/e}} &= n_{lsu} - k \\
 k &= 1/5(n_{esa} + n_{lsa} + n_{esu} + n_{lsu})
 \end{aligned}$$

boundary conditions:

$$\begin{aligned}
 n_{emf} ; n_{lmf} ; n_{esa} ; n_{lsa} ; n_{esu} ; n_{lsu} &\geq 0 \text{ (a whole number)} \\
 n_{emf} ; n_{lmf} &\geq k \\
 n_{esa} ; n_{esu} &= k \\
 k &\leq n_{lsa} ; n_{lsu} \leq 2k \\
 n_{esa} + n_{lsa} + n_{esu} + n_{lsu} &\equiv 0 \pmod{5}
 \end{aligned}$$

- k [-] a whole constant
- n_B [-] number of basic groups
- n_{mf} [-] number of duties on every monday to friday
- n_{sa} [-] number of duties on saturday
- n_{su} [-] number of duties on sunday and public holiday

number of week	su	mo	tu	we	th	fr	sa
B 1							
1.	day-off						day-off
B 6 (5)							
1.	day-off	day-off					
2.		day-off	day-off				
3.			day-off	day-off			
4.				day-off	day-off		
5.					day-off	day-off	
6.						day-off	day-off

it goes:

$$n_{B1} = n_{mf} - 4 n_{B6(5)}$$

$$n_{B6(5)} = 1/5 n_{sa} = 1/5 n_{su}$$

boundary conditions:

$$n_{mf} ; n_{sa} ; n_{su} \geq 0 \text{ (a whole number)}$$

$$n_{mf} \geq 4/5 n_{sa}$$

$$n_{mf} \geq 4/5 n_{su}$$

$$n_{sa} ; n_{su} \equiv 0 \pmod{5}$$

- n_B [-] number of basic groups
- n_{mf} [-] number of duties on every monday to friday
- n_{sa} [-] number of duties on saturday
- n_{su} [-] number of duties on sunday and public holiday

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monday – friday:

duty no.	train	begin and end working time	working time
1	1/3.	3.56 – 12.06	8:10
2	1/6.	4.14 – 12.51	8:37
3	1/7.	4.34 – 13.06	8:32
4	1/8.	4.49 – 13.04	8:15
5	11/1. + 1/7.	4.56 – 7.59 + 12.56 – 16.49	6:56
6	11/2. + 11/3.	5.11 – 8.14 + 15.11 – 18.14	6:06
7	11/3. + 1/6.	5.26 – 7.44 + 12.41 – 16.51	6:28
8	1/3.	11.56 – 19.49	7:53
9	11/1.	14.41 – 18.29	3:48
10	1/8.	12.54 – 19.04	6:10
11	11/2. + 1/3.	14.56 – 18.44 + 19.39 – 0.11	9:15
12	1/7.	16.39 – 1.18	8:39
13	1/6.	16.41 – 0.48	8:07
14	1/8.	18.54 – 4.21	9:27

saturday, sunday:

duty no.	train	begin and end working time	working time
21	1/3.	3.56 – 12.06	8:10
22	1/6.	4.14 – 12.51	8:37
23	1/7. + 1/8.	4.34 – 8.49 + 8.49 – 13.04	8:30
24	1/7.	8.39 – 17.06	8:27
25	1/3.	11.56 – 17.49	5:53
26	1/6.	12.41 – 18.34	5:53
27	1/8.	12.54 – 19.04	6:10
28	1/7.	16.56 – 1.18	8:22
29	1/3.	17.39 – 0.11	6:32
30	1/6.	18.24 – 0.48	6:24
31	1/8.	18.54 – 4.21	9:27

You have the duties number 1 to 14 and 21 to 31. Create a duty roster with weekly cycle. The first duty after days-off has to start as late as possible, the last one before days-off has to end as early as possible. The rest period between two duties may never be smaller than 10 hours.

Steps:

Selektion

-select the type of duty roster divided by rest period (**shift similarly, fast rotation** or **slow rotation**)

Calculation

- divide the duties evenly into **early** and **late** duties and include the necessary **buffer duties**
- calculate the **number of** 3, 4 or 6 weekly **basic groups** based on the number of weekend-duties
- include the missing duties Monday - Friday by including a sufficient number of one week basic groups
- compose the **whole duty roster**

Putting down

- **group the duties**, pay attention to the minimal rest period between two duties
- correct the whole duty roster, if necessary
- put all **duties into the finished roster**

monday – friday:

duty no.	train	begin and end working time	working time
1	1/3.	3.56 – 12.06	8:10
1.1	on-call duty	3.56 – 12.06	8:10
1.2	spare duty	(3.56 – 13.06)	7:37
2	1/6.	4.14 – 12.51	8:37
3	1/7.	4.34 – 13.06	8:32
4	1/8.	4.49 – 13.04	8:15
5	11/1. + 1/7.	4.56 – 7.59 + 12.56 – 16.49	6:56
6	11/2. + 11/3.	5.11 – 8.14 + 15.11 – 18.14	6:06
7	11/3. + 1/6.	5.26 – 7.44 + 12.41 – 16.51	6:28
8	1/3.	11.56 – 19.49	7:53
8.1	on-call duty	11.56 – 19.15	7:19
8.2	spare duty	(11.56 – 4.21)	7:37
9	11/1.	14.41 – 18.29	3:48
10	1/8.	12.54 – 19.04	6:10
11	11/2. + 1/3.	14.56 – 18.44 + 19.39 – 0.11	9:15
12	1/7.	16.39 – 1.18	8:39
13	1/6.	16.41 – 0.48	8:07
14	1/8.	18.54 – 4.21	9:27

saturday, sunday:

duty no.	train	begin and end working time	working time
21	1/3.	3.56 – 12.06	8:10
21.1	on-call duty	3.56 – 13.04	9:08
21.2	spare duty	(3.56 – 17.06)	7:37
22	1/6.	4.14 – 12.51	8:37
23	1/7. + 1/8.	4.34 – 8.49 + 8.49 – 13.04	8:30
24	1/7.	8.39 – 17.06	8:27
25	1/3.	11.56 – 17.49	5:53
25.1	on-call duty	11.56 – 19.24	7:28
25.2	spare duty	(11.56 – 4.21)	7:37
26	1/6.	12.41 – 18.34	5:53
27	1/8.	12.54 – 19.04	6:10
28	1/7.	16.56 – 1.18	8:22
29	1/3.	17.39 – 0.11	6:32
30	1/6.	18.24 – 0.48	6:24
31	1/8.	18.54 – 4.21	9:27

number of week	su	mo	tu	we	th	fr	sa
1.	day-off						day-off
2.	day-off	day-off					
3.		day-off	day-off				
4.			day-off	day-off			
5.				day-off	day-off		
6.					day-off	day-off	
7.						day-off	day-off
8.	day-off						day-off
9.	day-off						day-off
10.	day-off	day-off					
11.		day-off	day-off				
12.			day-off	day-off			
13.				day-off	day-off		
14.					day-off	day-off	
15.						day-off	day-off
16.	day-off						day-off
17.	day-off						day-off
18.	day-off	day-off					
19.		day-off	day-off				
20.			day-off	day-off			
21.				day-off	day-off		
22.					day-off	day-off	
23.						day-off	day-off
24.	day-off						day-off

number of week	su	mo	tu	we	th	fr	sa
1.	day-off						day-off
2.	day-off	day-off					
3.		day-off	day-off				
4.			day-off	day-off			
5.				day-off	day-off		
6.					day-off	day-off	
7.						day-off	day-off
8.	day-off						day-off
9.	day-off						day-off
10.	day-off	day-off					
11.		day-off	day-off				
12.			day-off	day-off			
13.				day-off	day-off		
14.					day-off	day-off	
15.						day-off	day-off
16.	day-off						day-off
17.	day-off						day-off
18.	day-off	day-off					
19.		day-off	day-off				
20.			day-off	day-off			
21.				day-off	day-off		
22.					day-off	day-off	
23.						day-off	day-off
24.	day-off						day-off

number of week	su	mo	tu	we	th	fr	sa
1.	day-off						day-off
2.	day-off	day-off					
3.	day-off	day-off	day-off				
4.			day-off	day-off			
5.				day-off	day-off		
6.					day-off	day-off	
7.						day-off	day-off
8.							day-off
9.	day-off						day-off
10.	day-off	day-off					
11.	day-off	day-off	day-off				
12.			day-off	day-off			
13.				day-off	day-off		
14.					day-off	day-off	
15.						day-off	day-off
16.							day-off
17.	day-off						day-off
18.	day-off	day-off					
19.	day-off	day-off	day-off				
20.			day-off	day-off			
21.				day-off	day-off		
22.					day-off	day-off	
23.						day-off	day-off
24.							day-off

3 groups with ever 6 duties Monday to Friday and ever 5 duties Saturday and Sunday:

I			II			III			IV			V			VI		
18.54	14	4.21	14.56	11	0.11	11.56	8.1	19.15	5.26	7	16.51	4.34	3	13.06	4.14	2	12.51
18.54	31	4.21	16.56	28	1.18	12.54	27	19.04	8.39	24	17.06	3.56	21.1	13.04			
16.41	13	0.48	(11.56)	8.2	(4.21)	14.41	9	18.29	4.56	5	16.49	(3.56)	1.2	(13.06)	3.56	1	12.06
18.24	30	0.48	(11.56)	25.2	(4.21)	12.41	26	18.34	4.34	23	13.04	3.56	21	12.06			
16.39	12	1.18	11.56	8	19.49	12.54	10	19.04	5.11	6	18.14	4.49	4	13.04	3.56	1.1	12.06
17.39	29	0.11	11.56	25.1	19.24	11.56	25	17.49	(3.56)	21.2	(17.06)	4.14	22	12.51			

number of week	su	mo	tu	we	th	fr	sa
1.	day-off	14	11	8.1	7	3	day-off
2.	day-off	day-off	13	8.2	9	5	21
3.	day-off	day-off	day-off	12	8	10	21.2
4.	22	1.1	day-off	day-off	14	11	27
5.	24	3	2	day-off	day-off	13	25.2
6.	26	5	1.2	1	day-off	day-off	29
7.	25.1	10	6	4	1.1	day-off	day-off
8.	31	11	8.1	7	3	2	day-off
9.	day-off	13	8.2	9	5	1.2	day-off
10.	day-off	day-off	12	8	10	6	22
11.	day-off	day-off	day-off	14	11	8.1	24
12.	21.1	2	day-off	day-off	13	8.2	26
13.	23	1.2	1	day-off	day-off	12	25.1
14.	25	6	4	1.1	day-off	day-off	31
15.	28	8.1	7	3	2	day-off	day-off
16.	30	8.2	9	5	1.2	1	day-off
17.	day-off	12	8	10	6	4	day-off
18.	day-off	day-off	14	11	8.1	7	21.1
19.	day-off	day-off	day-off	13	8.2	9	23
20.	21	1	day-off	day-off	12	8	25
21.	21.2	4	1.1	day-off	day-off	14	28
22.	27	7	3	2	day-off	day-off	30
23.	25.2	9	5	1.2	1	day-off	day-off
24.	29	8	10	6	4	1.1	day-off

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